

STUDENTID NO										

MULTIMEDIA UNIVERSITY

FINAL EXAMINATION

TRIMESTER 1, 2019/2020

PEM0044 - ESSENTIAL MATHEMATICS

(All sections / Groups)

15 OCTOBER 2019 2.30 p.m. - 4.30 p.m. (2 Hours)

INSTRUCTIONS TO STUDENTS

- 1. This question paper consists of FOUR (4) printed pages with 4 questions only, excluding the cover page.
- 2. Answer all FOUR (4) questions.
- 3. Write all your answers in the answer booklet provided. All necessary workings MUST be shown.
- 4. The formula sheet is attached at the end of this question paper.

Question 1 (25 Marks)

- (a) Simplify the following expression.
 - $(i) \qquad \frac{\left(3x^2y^7\right)^2}{3x}$

[2 marks]

(ii)
$$\sqrt[3]{\frac{2}{m^2n}}$$

[4 marks]

- (b) Solve the following equation and inequality.
 - (i) 5(3x+1)+2(x-2)=4x+3

[3 marks]

(ii)
$$2(x+3) \le -4(x-2)$$

[3 marks]

(c) Use the quadratic formula to solve the following equation.

$$x^2 - x - 2 = 0$$

[6 marks]

(d) Find an equation of the straight line that passes through point (5, 2) and (8, 1). Then, sketch a graph.

[7 marks]

Continued...

Question 2 (25 Marks)

(a) Given that $\mathbf{A} = \begin{bmatrix} 1 & 4 \\ 2 & 7 \end{bmatrix}$, and $\mathbf{B} = \begin{bmatrix} -2 & -4 \\ 3 & 0 \end{bmatrix}$. Find $\mathbf{A}^T + 3\mathbf{B}^T$.

[5 marks]

(b) Consider the following system of equations.

$$x + 2y + z = 2$$

$$x+4v+z=4$$

$$5x + y + 2z = 1$$

- (i) Write the system of equation above in a form Ax = B.
- (ii) Find A^{-1} .

[3 marks]

(iii) Find the value of x, y and z.

[14 marks]

[3 marks]

Question 3 (20 Marks)

- (a) Given the arithmetic sequence is 27, 22, 17,
 - (i) Find the first term and the common difference.

[3 marks]

(ii) Find the sum of the first 11 terms.

[3 marks]

(b) The seventh term of an arithmetic sequence is 20 and the sum of the first ten terms is 155. Find the common difference.

[7 marks]

- (c) Given the geometric sequence is 81, 27, 9,
 - (i) Find the 12 term.

[4 marks]

(ii) Find the sum of the first 50 terms.

[3 marks]

Continued...

Question 4 (30 Marks)

(a) Find f'''(x) if $f(x) = 3 - x^2 + x^3 - 2x^4$.

[6 marks]

- (b) Find the first derivative of the following functions. Simplify your answer.
 - (i) $f(x) = (x+4)\left(\frac{2x^2+1}{2x-1}\right)$

[9 marks]

(ii) $f(x) = \frac{9}{\sqrt[3]{x^2 + \pi}}$

[4 marks]

- (c) Evaluate the following indefinite integrals:
 - (i) $\int \left(\frac{2}{x^3} + 1 3\sqrt[3]{x^2}\right) dx$

[5 marks]

(ii) $\int 4x^3 \sqrt{1+x^4} \ dx$

[6 marks]

End of Page.

Summary of Formulas

1. Basic Rules of Differentiation

i)
$$f'(x) = 0$$

ii)
$$f'(x) = nx^{n-1}$$

iii)
$$cf(x) = cf'(x)$$

iv)
$$f(x) \pm g(x) = f'(x) \pm g'(x)$$

v)
$$f'(x) = u \frac{dv}{dx} + v \frac{du}{dx}$$

vi)
$$f'(x) = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{[v]^2}$$

vii) Chain rule:
$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx}$$

viii) General power rule: Derive $[f(x)]^n = n[f(x)]^{n-1} f'(x)$

2. Basic Rules of Integration

i)
$$\int k \ du = ku + C$$

ii)
$$\int u'' du = \frac{u^{n+1}}{n+1} + C$$

iii)
$$\int k f(u) du = k \int f(u) du$$

iv)
$$\int [f(u) \pm g(u)] du = \int f(u) du + \int g(u) du$$